## Impact of Galileo on geodetic positioning applications

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The impact of Galileo, the proposed European satellite navigation system, on geodetic positioning and zenith delay estimation is discussed.

Galileo and the modernized GPS system will provide more and better signals on both existing and new frequencies, resulting in improved observations.

	carrier	code	comp.	chip-rate	data	remarks
L1	1575.42	P(Y)	I(cos)	10.23 Mcps	yes	
	MHZ	CA	Q(sin)	1.023 Mcps	yes	
		М	Binary O	ffset Carrier		2004 onwards
L2	1227.60	P(Y)	I(cos)	10.23 Mcps	no	
	MHz	CS	Q(sin)	1.023 Mcps	TDMA	2004 onwards
		М	Binary O	Binary Offset Carrier		retrofit IIR
L5	1176.45 MHz	P-like	I(sin)	10.23 Mcps	yes	2006 onwards
		P-like	Q(sin)	10.23 Mcps	pilot	Block IIF

Contemporary (bold) and modernized GPS signals. GPS: 24 nominal satellites, circular orbits 20,200 km, orbital period  $11^h58^m$ , inclination  $55^0$ , 6 planes.

	carrier	code	comp	chip-rate	data	service
E2-	1575.42	BOC[2,2]	I(cos)	2.026 Mcps	200sps	OS/SAS
L1-	MHZ	or[1,1]	Q(sin)	2.026 Mcps	pilot	
E1		BOC[14,2]	PRS			
E5a	1176.45	BPSK	I(sin)	10.23 Mcps	50sps	OS/SAS
= L5	MHz	(P-like)	Q(sin)	10.23 Mcps	pilot	
E5b	1207.14	BPSK	I(sin)	10.23 Mcps	500sps	OS/SAS/
	MHz	(P-like)	Q(sin)	10.23 Mcps	pilot	CS
E6 1278.75		BPSK	I(sin)	5.115 Mcps	1000sps	CS
	MHz	(CA-like)	Q(sin)	5.115 Mcps	pilot	
		BOC[10,5]		5.115 Mcps	1000sps	PRS

Planned Galileo signals and services (subject to change). Galileo: 27 nominal  $\pm$  3 spare satellites, circular orbits 23,616 km, orbital period  $14^h24^m$ , inclination  $56^0$ , 3 orbital planes (OS: Open Service).

The new signals on L5 result in a 24% improvement in precision of the ionosphere free linear combination (IF) if used instead of L2, or 30% if all three frequencies are used, under the assumption that the carrier phase observations have the same accuracy as GPS today.

The geometry free linear combination (I1) is improved likewise.

Two frequency GPS L1&L2	
$\phi_F = 2.5457 \ \phi_{L1} - 1.5457 \ \phi_{L2}$	$\sigma_{\rm F}$ = 2.98 $\sigma_{\rm D}$
$\phi_{11} = -1.5457 \ \phi_{L1} + 1.5457 \ \phi_{L2}$	$\sigma_{i1}$ = 2.19 $\sigma_{0}$
Two frequency GPS L1&L5	
$\phi_F = 2.2606 \ \phi_{L1} - 1.2606 \ \phi_{L5}$	$\sigma_{\rm F}$ = 2.59 $\sigma_{\rm D}$
$\phi_{L1} = -1.2606 \ \phi_{L1} + 1.2606 \ \phi_{L5}$	$\sigma_{i1}$ = 1.78 $\sigma_{0}$
Three frequency GPS L1,L2&L5	
$\phi_F = 2.3269 \ \phi_{L1} - 0.3596 \ \phi_{L2} - 0.9673 \ \phi_{L5}$	$\sigma_{\rm F}$ = 2.55 $\sigma_{\rm D}$
$\phi_{11} = -1.3470 \ \phi_{L1} + 0.4682 \ \phi_{L2} + 0.8788 \ \phi_{L5}$	$\sigma_{i1}$ = 1.68 $\sigma_{0}$
Two frequency GALILEO E2-L1-E1 & E5b	
$\phi_{if} = 2.3932 \; \phi_{L1} - 1.3932 \; \phi_{ESb}$	$\sigma_{if}$ = 2.77 $\sigma_{ij}$
$\phi_{i1} = -1.3932 \; \varphi_{i,1} + 1.3932 \; \varphi_{E5b}$	$\sigma_{11}$ = 1.97 $\sigma_{0}$
Two frequency GALILEO E2-L1-E1 & E5a	
$\phi_{if} = 2.2606 \; \phi_{L,i}  \; 1.2606 \; \phi_{ESa}$	$\sigma_{if}$ = 2.59 $\sigma_{0}$
$\phi_{i1} = -1.2606 \; \phi_{i.1} + 1.2606 \; \phi_{i.5a}$	$\sigma_{11}$ = 1.78 $\sigma_{0}$
Three frequency GALILEO E2-L1-E1, E5b & E5a	
$\phi_{if} = 2.3088 \; \phi_{Li}  \; 0.5063 \; \phi_{E5b}  \; 0.8024 \; \phi_{E5a}$	$\sigma_{if}$ = 2.50 $\sigma_{0}$
$\phi_{i1} = -1.3138 \; \phi_{L1} + 0.5584 \; \phi_{E5b} + 0.7553 \; \phi_{E5a}$	$\sigma_{i1}$ = 1.62 $\sigma_{0}$

The main improvement comes from having additional satellites, as is illustrated by the following conservative simulation experiments.

24 h data-set for:

- The Netherlands (52.22° N, 4.42 ° E)
- 24 GPS and 30 Galileo satellites
- 10° elevation cut-off angle

lonosphere free single diff. observation

- phase ( $\sigma\text{=}\sqrt{2}\text{*}9$  mm) & code ( $\sigma\text{=}\sqrt{2}\text{*}0.9$  m) Precise orbits (orbit errors neglected)

Estimated parameters:

- independent receiver clock errors for GPS and Galileo (1-2 per epoch)
- zenith delay (one per epoch)
- station position (static or kinematic)
- phase ambiguities (float and fixed)

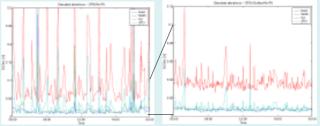
Satellite clock errors are taken care of by the single difference.

NEU [mm]		GPS/float			GPS/fixed			G&G/float			G&G/fixed			
		E	N	U	E	N	U	E	N	U	E	N	c	
Static		1.4	0,7	2,9	0,4	0,5	2.5	8,0	0,4	1.7	0,3	0,3	1,5	
Kinematic w/6 ZTD	medjan	10,8	11,7	24,3	8,7	11,0	22,9	6,1	7,3	14,5	5,7	7,1	14.1	
	mean	11,0	13.9	25,0	9,3	13,0	23,9	6,3	7,5	14.7	5,8	7,2	14.4	
	min	7,7	8,8	15,1	6,7	8,1	14,1	4,8	5,5	10,5	4,3	5,6	10,3	
	max	24,8	29,3	55,9	23,5	28,9	55,2	9,3	10,5	20,8	8,5	10,3	20,6	
Kinematic w/ZTD	medjan	13,0	14.9	73,1	10.5	13,4	70,6	6,6	7,7	35,7	6,0	7.4	35,0	
	mean	15,4	19,2	126,8	12,7	17.4	122,1	6,7	7.9	37,8	6,2	7,6	37,2	
	min	8,5	9,4	34,1	6,7	8,2	32,5	4,8	5,9	25,7	4,3	5,6	25,3	
	max	282,1	198.0	8830	278,1	194,2	8712	10.4	12,0	119,4	9,4	11.7	117,9	
ZTD Kinematic/float Kine						inematic/fixed			Static/float			Static /fixed		

Results: Standard deviation of estimated parameters in [mm].

| TTD | Kinematic/fibat | Kinematic/fited | Statik/fibat | Statik/

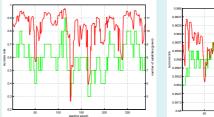
Ambiguity fixing was assumed to be 100% successful; success rates were not evaluated



Example of a simulation: Standard deviation of East, North, Height and ZTD for GPS (left) and GPS & GALILEO (right) for a kinematic receiver with float ambiguities.

St.Dev.Ratio	Roat Ambiguities				Fixed Ambiguities				Theoretical
St.Dev.Ratio	Е	N	U	ZTD	Е	N	٦	ZTD	benchmark
Static w/ ZTD	0.61	0.65	0.59	0.64	0.64	0.61	0.58	0.63	0.62
Kinematic w/o ZTD	0.56	0.62	0.60	-	0.65	0.64	0.62	-	0.51
Kinematic w/ ZTD	0.50	0.52	0.49	0.41	0.57	0.55	0.50	0.42	0.43

Ratio of standard deviations GPS & Galileo versus GPS only for different scenarios, showing the improvement in precision due to extra satellites.





Probability of successful single epoch ambiguity resolution (red line) for GPS (left) and GPS & Galileo (right) for a 24 hour period in the Netherlands, using all publicly available frequencies. The green line is the number of available satellites. The probability is increased by combining GPS with Galileo and using all available frequencies.

The improved redundancy of a dual GNSS system will make it possible to introduce additional parameters to reduce (systematic) errors and improve the accuracy even further. The improved accuracy will also make new applications possible, especially for moving receivers.

